

The Gaussian Process Prior VAE for Latent Dynamics from Pixels

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Research Question

- given videos of moving object $v_{1:T}$
- unsupervised learn latent $x_{1:T}, y_{1:T}$
- ~~graphical model prior~~ use a GP?
- Let's see on some toy data...

Generative Model

GP Prior NN+Bernoulli L'hood

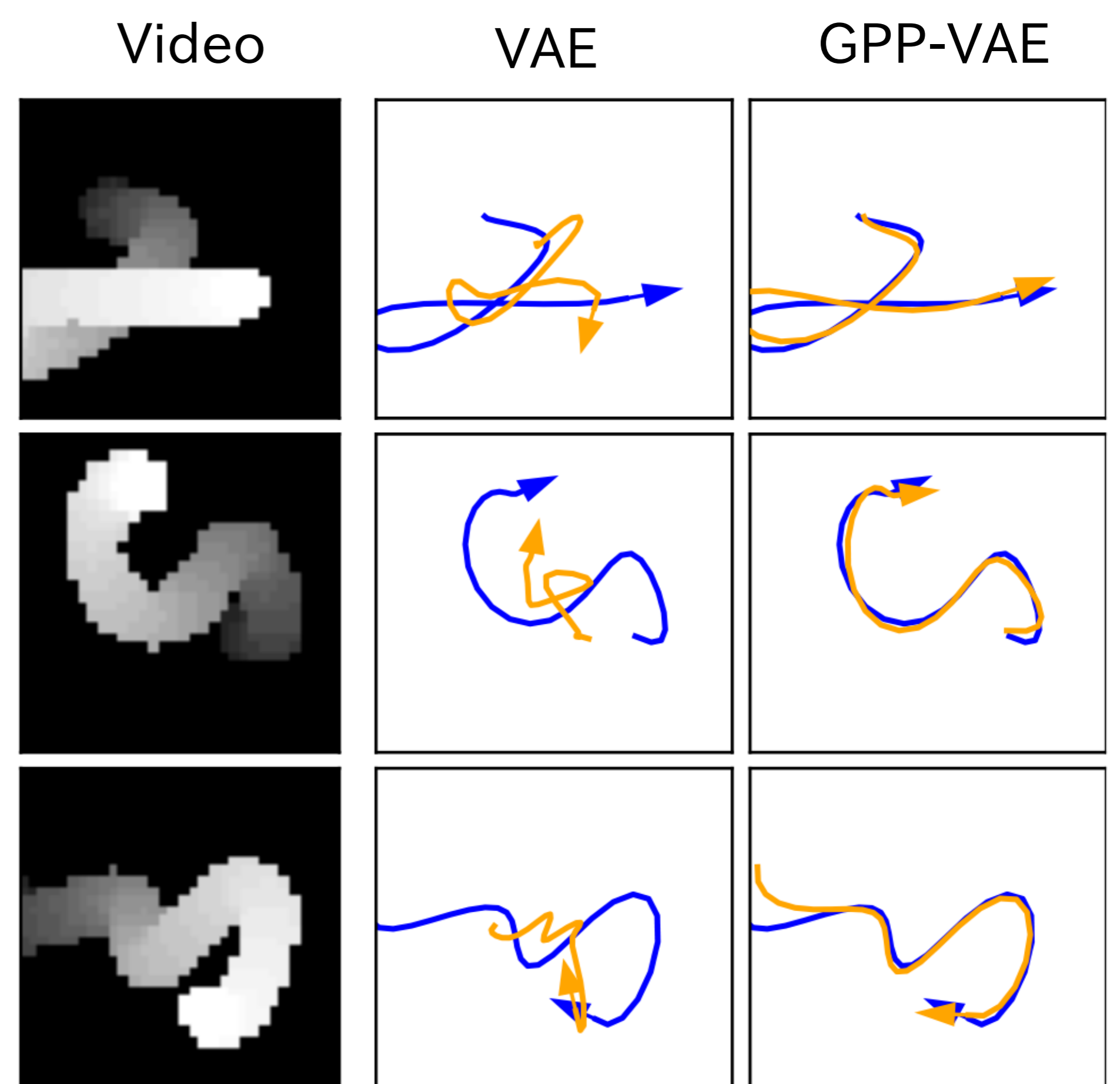
$x_{1:T}, y_{1:T}$ $v_{1:T}$

$\mathcal{GP}(x_{1:T}, y_{1:T})$ $\prod_{t=1}^T \mathcal{B}(v_t | p_\theta(x_t, y_t))$

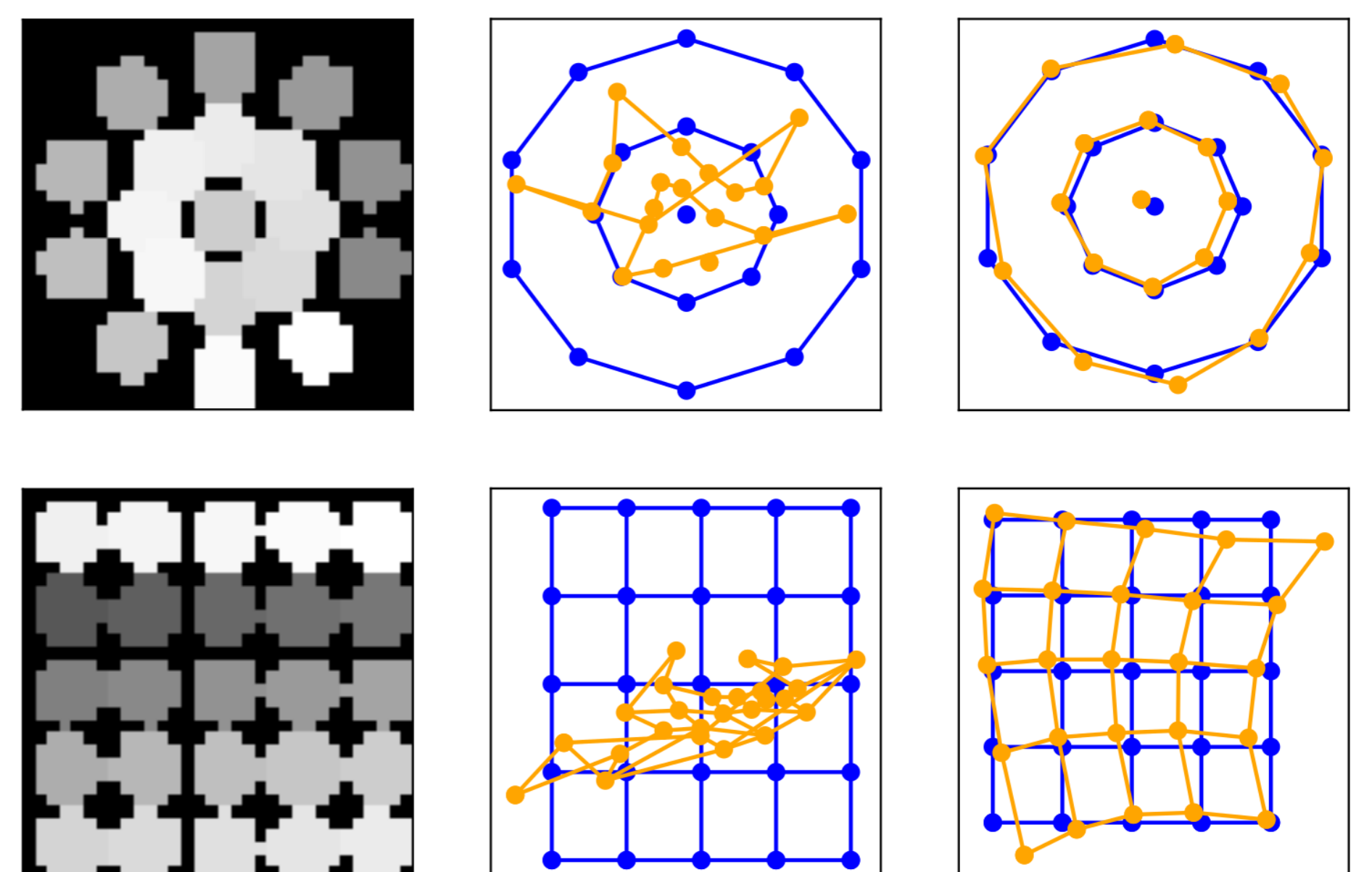
$\mathbb{P}[v_{1:T}, x_{1:T}, y_{1:T}] = \mathcal{GP}(x_{1:T}, y_{1:T}) \prod_{t=1}^T \mathcal{B}(v_t | p_\theta(x_t, y_t))$

Experiments

$$\mathbb{E}_q \left[\underbrace{\sum_{t \in \mathcal{I}} \log \mathcal{B}(v_t | p_\theta(x_t, y_t))}_{\text{swap "error"}} - \underbrace{\log q_\phi^*(x_t, y_t | v_t)}_{\text{GPR l'hood}} \right] + \log Z(v_{1:T})$$



How "Euclidean" is the latent space?

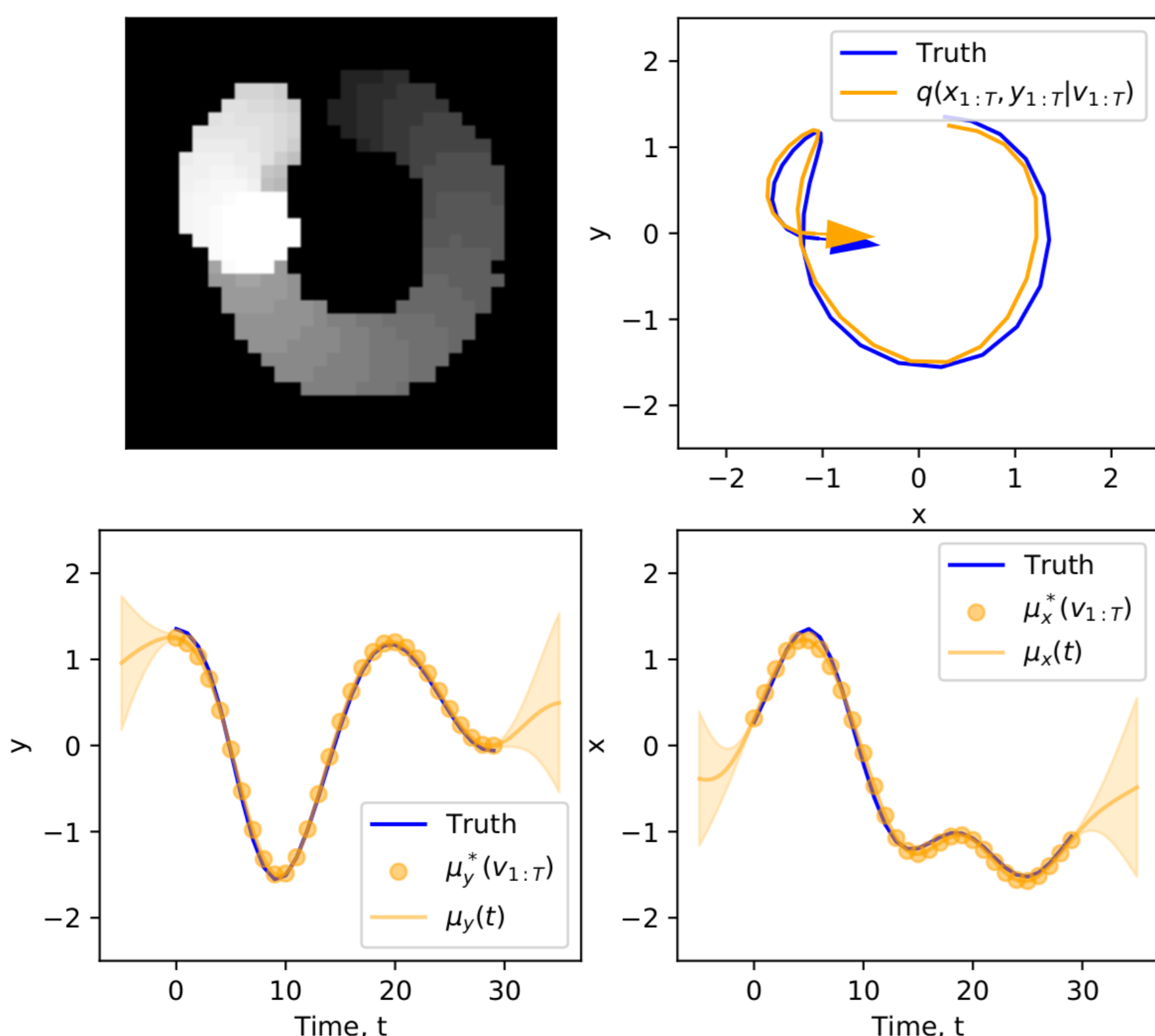


Ammortised Inference Model

1. take generative model
2. swap (annoying) likelihood with Gaussian with mean+var from network of image
3. do Gaussian process regression!

$$\mathcal{B}(v_t | p_\theta(x_t, y_t)) \rightarrow q_\phi^*(x_t, y_t | v_t) = \mathcal{N}(x_t | \mu_{x\phi}^*(v_t), \sigma_{x\phi}^{*2}(v_t))$$

$$q(x_{1:T}, y_{1:T} | v_{1:T}) = \frac{1}{Z(v_{1:T})} \prod_{t=1}^T q_\phi^*(x_t, y_t | v_t) \mathcal{GP}(x_{1:T}, y_{1:T})$$



Many open questions

- model-mismatch: non GP-synthetic-data
- kernels: periodic/Brownian/Matern
- Bayesian forecasting/planning?
- reduce cubic computation of inference